## CSE 401 - Ambiguity Worksheet - Week 2 - Solutions

1. Consider the following syntax for expressions involving addition and field selection:
```
expr ::= expr + field
expr ::= field
field ::= expr . id
field ::= id
```

a) Show that this grammar is ambiguous.

Here are two derivations of id+id.id:

b) Give an unambiguous context-free grammar that fixes the problem(s) with the grammar in part (a) and generates expressions with id, field selection, and addition. As in Java, field selection should have higher precedence than addition and both field selection and addition should be left-associative (i.e. $a+b+c$ means $(a+b)+c$ ).

The problem is in the first rule for field, which creates an ambiguous precedence. Here is a reasonably simple fix.

$$
\begin{aligned}
& \operatorname{expr}::=\text { expr }+ \text { field } \\
& \text { expr }::=\text { field } \\
& \text { field }::=\text { field } . \text { id } \\
& \text { field }::=\text { id }
\end{aligned}
$$

