



CONCOLIC TESTING

Pınar Sağlam

Elided to examples only

Example

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
int f(int v) {
    return 2*v + 1;
}
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

- Random Test Driver:
 - random memory graph reachable from p
 - random value for x
- Probability of reaching `abort()` is extremely low

CUTE Approach

```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;  
int f(int v) {  
    return 2*v + 1;  
}  
int testme(cell *p, int x) {  
    if (x > 0)  
        if (p != NULL)  
            if (f(x) == p->v)  
                if (p->next == p)  
                    abort();  
    return 0;  
}
```

Concrete
Execution

Symbolic
Execution

concrete
state

symbolic
state

constraints

p
↓
NULL, x=236

p=p₀, x=x₀



CUTE Approach

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Concrete
Execution

Symbolic
Execution

concrete
state

symbolic
state

constraints

p
↓
NULL, x=236

$p=p_0, x=x_0$



CUTE Approach

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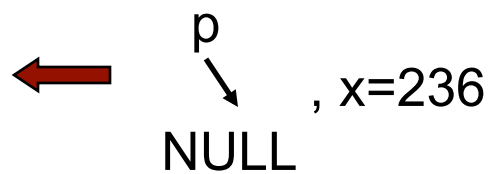
Concrete
Execution

Symbolic
Execution

concrete
state

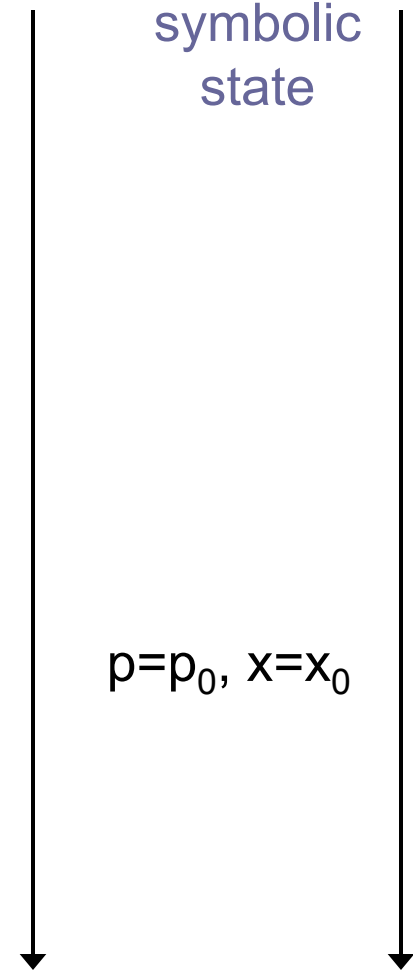
symbolic
state

constraints



$p=p_0, x=x_0$

$x_0 > 0$



CUTE Approach

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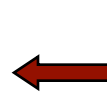
Concrete Execution

Symbolic Execution

concrete state

symbolic state

constraints



p
↓
NULL, x=236

p=p₀, x=x₀

x₀>0
!(p₀!=NULL)

CUTE Approach

Concrete Execution

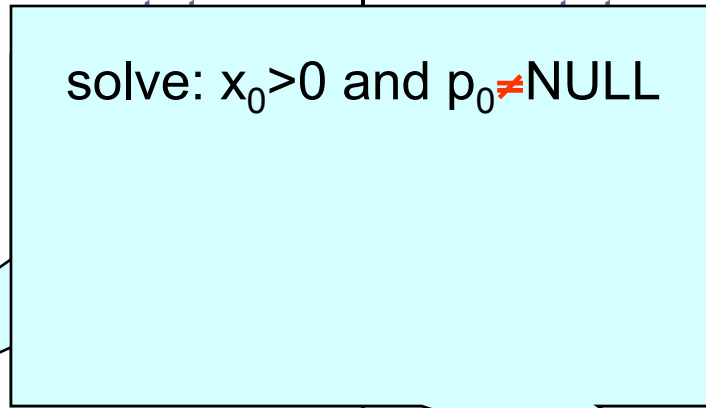
Symbolic Execution

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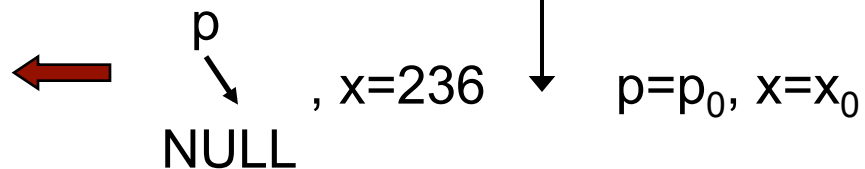
concrete

symbolic

constraints



$x_0 > 0$
 $p_0 = \text{NULL}$



CUTE Approach

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int f(int v) {
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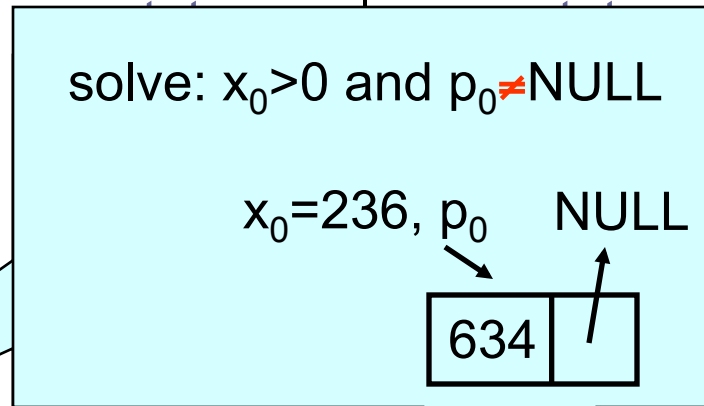
Concrete Execution

Symbolic Execution

concrete

symbolic

constraints



$x_0 > 0$
 $p_0 = \text{NULL}$

$p \rightarrow \text{NULL}$, $x = 236$

$p = p_0, x = x_0$

CUTE Approach

Concrete Execution

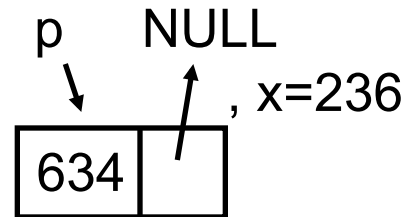
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```

concrete state

symbolic state

constraints



$p=p_0, x=x_0,$
 $p \rightarrow v = v_0,$
 $p \rightarrow next = n_0$



CUTE Approach

Concrete Execution

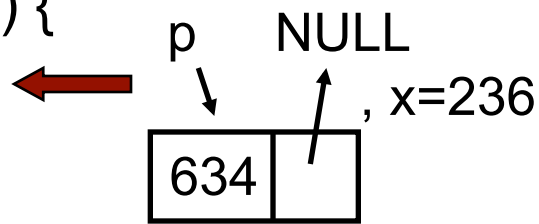
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concrete state

symbolic state

constraints



$p=p_0, x=x_0,$
 $p->v =v_0,$
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$x_0 > 0$

CUTE Approach

Concrete Execution

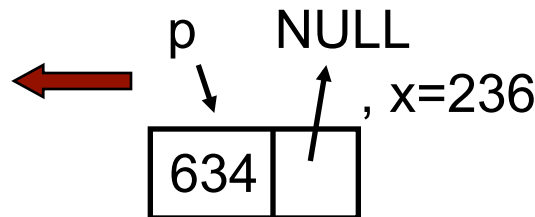
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concrete state

symbolic state

constraints



$p=p_0, x=x_0,$
 $p->v =v_0,$
 $p->next=n_0$

$x_0 > 0$
 $p_0 \neq NULL$

CUTE Approach

Concrete Execution

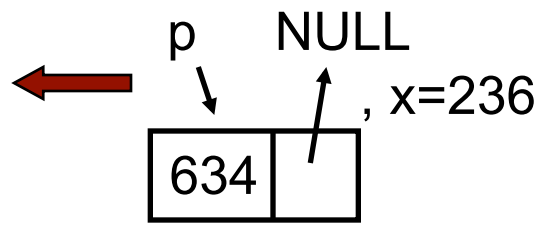
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concrete state

symbolic state

constraints



$p=p_0, x=x_0,$
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$x_0 > 0$
 $p_0 \neq \text{NULL}$
 $2x_0 + 1 \neq v_0$

CUTE Approach

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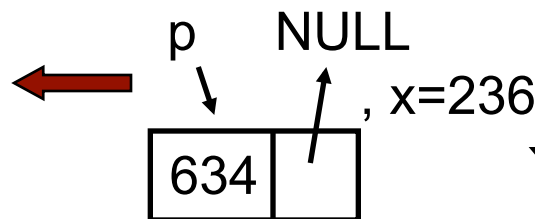
Concrete Execution

Symbolic Execution

concrete state

symbolic state

constraints



$p = p_0, x = x_0,$
 $p \rightarrow v = v_0,$
 $p \rightarrow next = n_0$

$x_0 > 0$
 $p_0 \neq \text{NULL}$
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CUTE Approach

Concrete Execution

Symbolic Execution

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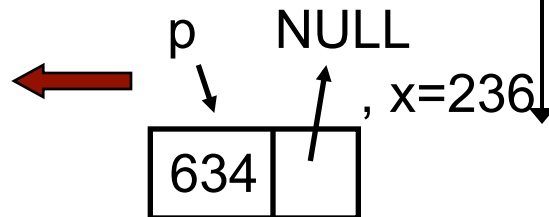
concrete

symbolic

constraints

solve: $x_0 > 0$ and $p_0 \neq \text{NULL}$
and $2x_0 + 1 = v_0$

$x_0 > 0$
 $p_0 \neq \text{NULL}$
 $2x_0 + 1 \neq v_0$



$p = p_0, x = x_0,$
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CUTE Approach

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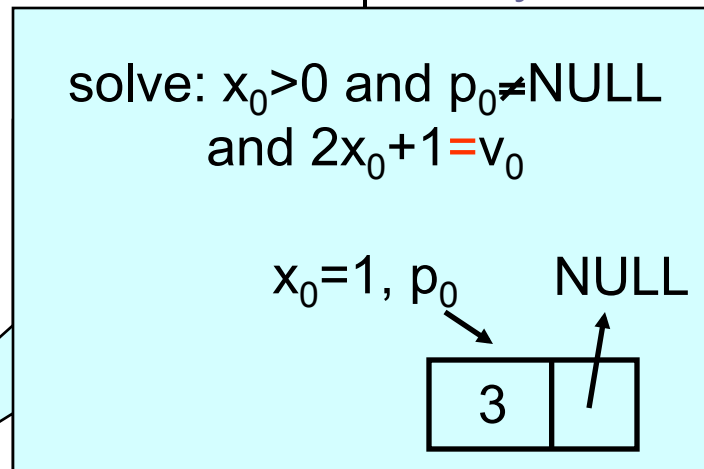
Concrete Execution

Symbolic Execution

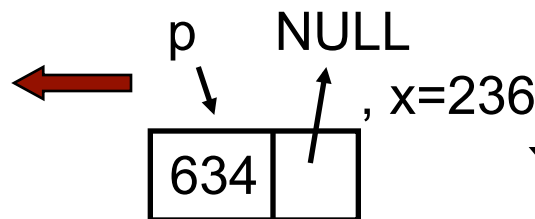
concrete

symbolic

constraints



$x_0 > 0$
 $p_0 \neq \text{NULL}$
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$p = p_0, x = x_0,$
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CUTE Approach

Concrete Execution

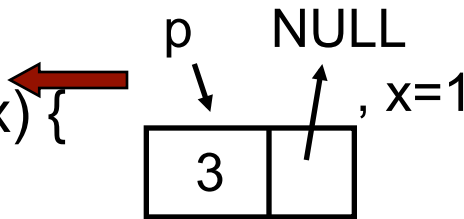
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```

concrete state

symbolic state

constraints



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 $p \rightarrow v = v_0,$
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CUTE Approach

Concrete Execution

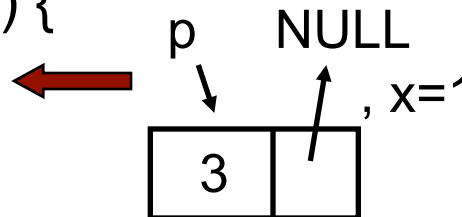
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concrete state

symbolic state

constraints



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$x_0 > 0$

CUTE Approach

Concrete Execution

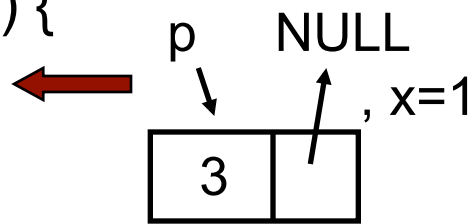
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concrete state

symbolic state

constraints

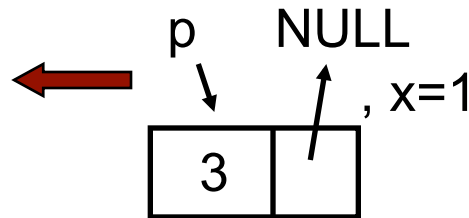


$p=p_0, x=x_0,$
 $p \rightarrow v = v_0,$
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$x_0 > 0$
 $p_0 \neq NULL$

CUTE Approach

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Concrete Execution

Symbolic Execution

concrete state

symbolic state

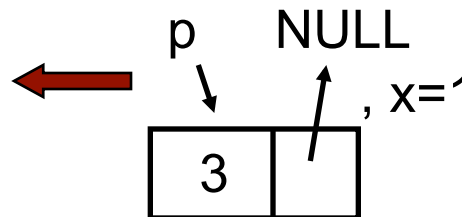
constraints

$p = p_0, x = x_0,$
 $p \rightarrow v = v_0,$
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$x_0 > 0$
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 $2x_0 + 1 = v_0$

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Concrete Execution

Symbolic Execution

concrete state

symbolic state

constraints

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$x_0 > 0$
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Concrete
Execution

Symbolic
Execution

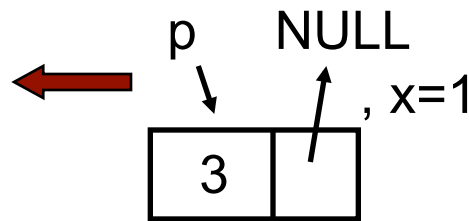
concrete
state

symbolic
state

constraints

$x_0 > 0$
 $p_0 \neq \text{NULL}$
 $2x_0 + 1 = v_0$
 $n_0 \neq p_0$

$p = p_0, x = x_0,$
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Concrete Execution

Symbolic Execution

concrete state

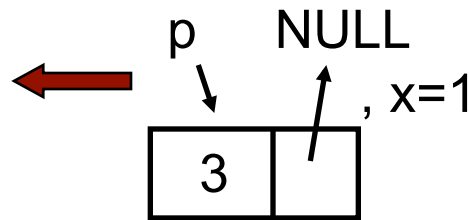
symbolic state

constraints

solve: $x_0 > 0$ and $p_0 \neq \text{NULL}$
and $2x_0 + 1 = v_0$ and $n_0 = p_0$

$x_0 > 0$
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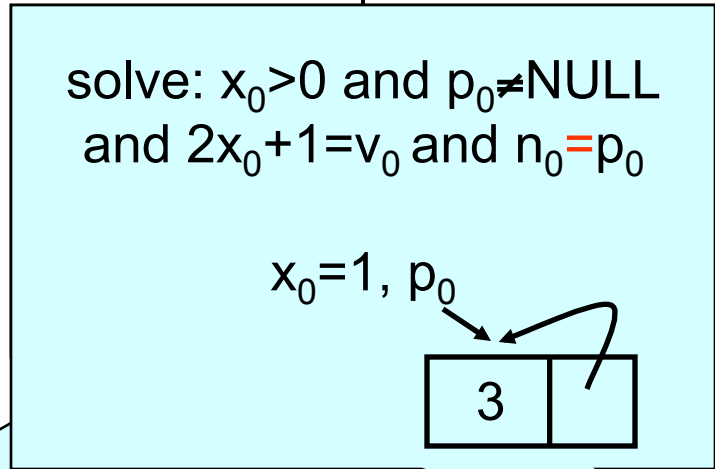
Concrete Execution

Symbolic Execution

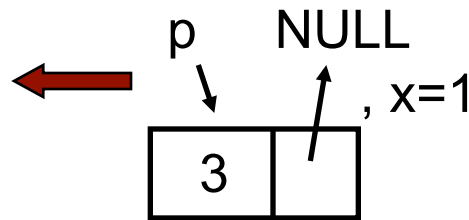
concrete state

symbolic state

constraints



$x_0 > 0$
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$p = p_0, x = x_0,$
 $p \rightarrow v = v_0,$
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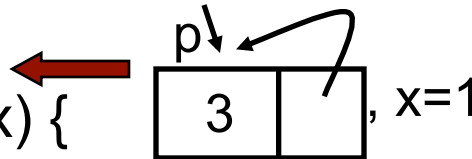
CUTE Approach

Concrete Execution

Symbolic Execution

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concrete state



symbolic state

$p=p_0, x=x_0,$
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constraints



CUTE Approach

Concrete Execution

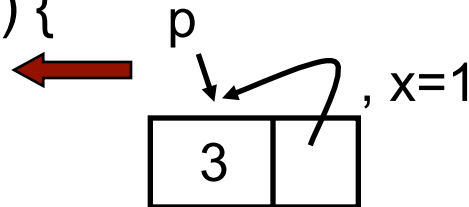
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concrete state

symbolic state

constraints

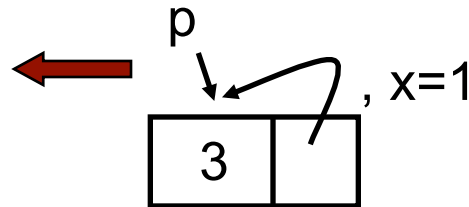


$p=p_0, x=x_0,$
 $p \rightarrow v = v_0,$
 $p \rightarrow next = n_0$

$x_0 > 0$

CUTE Approach

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Concrete Execution

Symbolic Execution

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symbolic state

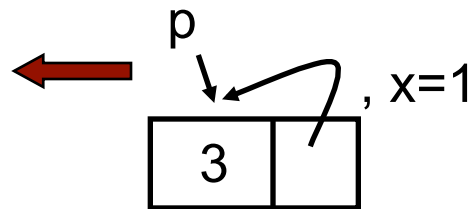
constraints

$p=p_0, x=x_0,$
 $p \rightarrow v = v_0,$
 $p \rightarrow next = n_0$

$x_0 > 0$
 $p_0 \neq \text{NULL}$

CUTE Approach

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}
```

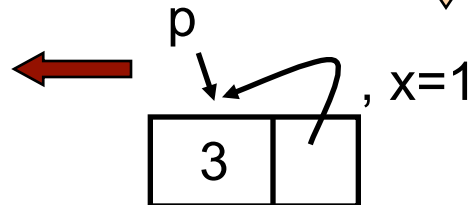
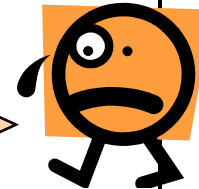
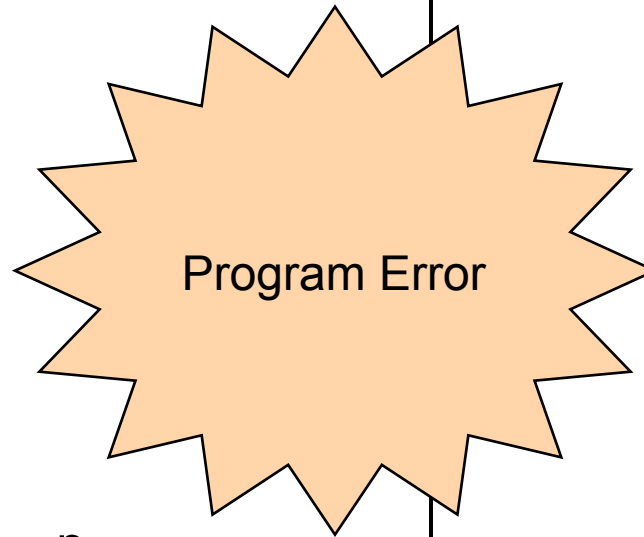
Concrete Execution

Symbolic Execution

concrete state

symbolic state

constraints



$p = p_0, x = x_0,$
 $p \rightarrow v = v_0,$
 $p \rightarrow next = n_0$

$x_0 > 0$
 $p_0 \neq \text{NULL}$
 $2x_0 + 1 = v_0$
 $n_0 = p_0$

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int  
    y){  
    z = x*x*x + 3*x*x + 9;  
    if(z != y){  
        printf("Good branch");  
    } else {  
        printf("Bad branch");  
        abort();  
    }  
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int
  y){
  z = x*x*x + 3*x*x + 9;
  if(z != y){
    printf("Good branch");
  } else {
    printf("Bad branch");
    abort();
  }
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x^3 + 3x^2 + 9$
- take then branch with constraint $x^3 + 3x^2 + 9 = y$!

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int
    y){
    z = x*x*x + 3*x*x + 9;
    if(z != y){
        printf("Good branch");
    } else {
        printf("Bad branch");
        abort();
    }
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x^3 + 3x^2 + 9$
- take then branch with constraint $x^3 + 3x^2 + 9 \neq y$
- solve $x^3 + 3x^2 + 9 = y$ to take else branch
- Don't know how to solve !!
 - **Stuck ?**

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int
    y){
    z = x*x*x + 3*x*x + 9;
    if(z != y){
        printf("Good branch");
    } else {
        printf("Bad branch");
        abort();
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}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x^3 + 3x^2 + 9$
- take then branch with constraint $x^3 + 3x^2 + 9 \neq y$
- solve $x^3 + 3x^2 + 9 = y$ to take else branch
- Don't know how to solve !!
 - Stuck ?
 - NO : CUTE handles this smartly

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int  
    y){  
    z = x*x*x + 3*x*x + 9;  
    if(z != y){  
        printf("Good branch");  
    } else {  
        printf("Bad branch");  
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    }  
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver

Simultaneous Symbolic & Concrete Execution

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void again_test_me(int x,int  
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    z = x*x*x + 3*x*x + 9;  
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    } else {  
        printf("Bad branch");  
        abort();  
    }  
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x + 9$
 - cannot handle symbolic value of z

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int  
    y){  
    z = x*x*x + 3*x*x + 9;  
    if(z != y){  
        printf("Good branch");  
    } else {  
        printf("Bad branch");  
        abort();  
    }  
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x + 9$
 - cannot handle symbolic value of z
 - make symbolic $z = 9$ and proceed

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int  
    y){  
    z = x*x*x + 3*x*x + 9;  
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```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x + 9$
 - cannot handle symbolic value of z
 - make symbolic $z = 9$ and proceed
- take then branch with constraint $9 \neq y$

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int  
    y){  
    z = x*x*x + 3*x*x + 9;  
    if(z != y){  
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```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x + 9$
 - cannot handle symbolic value of z
 - make symbolic $z = 9$ and proceed
- take then branch with constraint $9 \neq y$
- solve $9 = y$ to take else branch
- execute next run with $x = -3$ and $y = 9$
 - **got error (reaches abort)**

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int  
y){  
z = x*x*x + 3*x*x + 9;  
if  
}  
}
```

Replace symbolic expression
by concrete value when
symbolic expression becomes
unmanageable (i.e. non-linear)

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x + 9$
 - cannot handle symbolic value of z
 - make symbolic $z = 9$ and proceed
- take then branch with constraint $9 \neq y$
- solve $9 = y$ to take else branch
- execute next run with $x = -3$ and $y = 9$
 - got error (reaches abort)