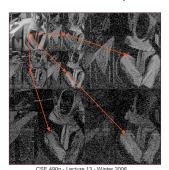
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SPIHT Group Testing

The Zero-Tree Method • Invented by Shapiro, 1993, and refined by Said and Pearlman, 1996. If a bit plane value in a low resolution subband is insignificant then it is likely that the corresponding values in higher subbands are also insignificant in the same bit plane. Such groups of insignificant values are called zero-trees.

Zero-Tree Example



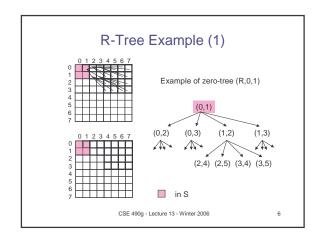
Values in a zero-tree are correlated.

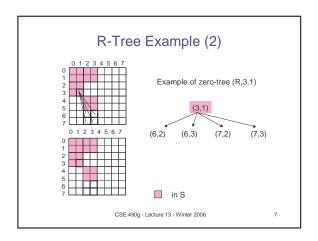
Simplified SPIHT Coding

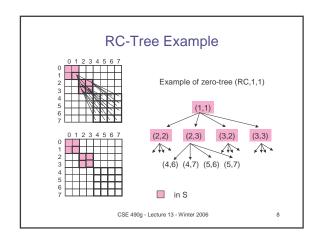
- Runs in passes one for each bit plane.
- C[i,j] is the coefficient at index (i,j) and C[i,j,k] is the k-th bit of C[i,j].
- Encoder maintains two data structures.
 - S, a list of indices (i,j) such that C[i,j] is declared significant in the current bit plane.
 - Z, a stack of zero trees of two types.
 - rootless (R)
 - root-and-childless (RC)
 - The nodes in a zero tree are insignificant in the current bit plane. (ignore root in R and root and children in RC)

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SPIHT Zero-Trees root is on the list S all other nodes are insignificant in current bit plane RC Each zero tree can be identified by its type and the index (i,j) of its root. CSE 490g - Lecture 13 - Winter 2006 5







Initialization of SPIHT

- The lowest subband indices are put into S.
 - If (i,j) in lowest subband then output sign (0 for and 1 for +) of C[i,j] and put (i,j) into S.
- A stack Z of zero trees is formed using the lowest resolution subband indices as roots.
 - If (i,j) in the lowest subband is a root of a zero tree of type R if i is odd or (i is even and j is odd).

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Iteration of SPIHT Encoder

We have list S of significant values and a stack Z of zero trees from the previous pass or the initialization. Significance Pass. while Z is not empty do T := pop(Z);if T has an index that becomes significant in bit plane k then output 1;

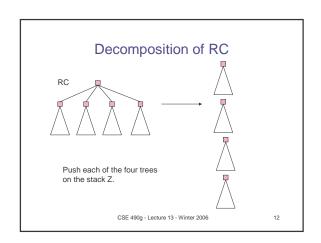
decompose(T);

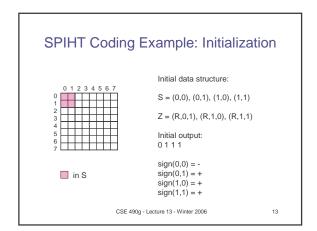
output 0;

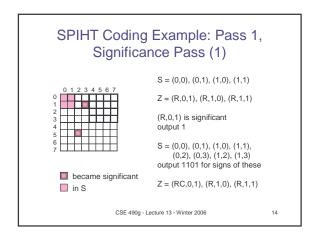
push T on Z' Z := Z'; {At this point all indices in zero trees in Z are insignificant} Refinement Pass for each (i,j) in S output the k-th significant bit, C[i,j,k].

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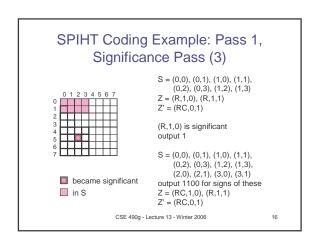
Decomposition of R Output the sign (0 for - and 1 for +) of each of the children of the root and put them in S. Push the RC tree on the stack Z. Exception is when tree has no grandchildren. In this case, the tree dies. CSE 490g - Lecture 13 - Winter 2006

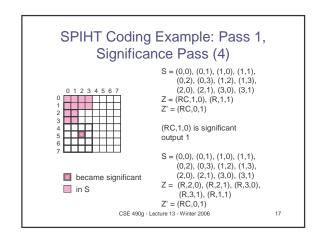


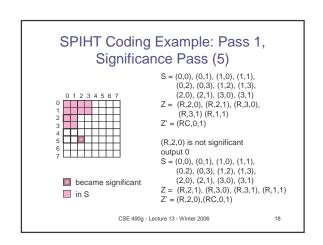




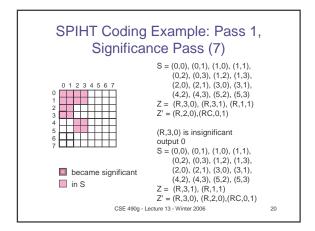
SPIHT Coding Example: Pass 1, Significance Pass (2) S = (0,0), (0,1), (1,0), (1,1), (0,2), (0,3), (1,2), (1,3) Z = (RC,0,1), (R,1,0), (R,1,1) (RC,0,1) is not significant output 0 S = (0,0), (0,1), (1,0), (1,1), (0,2), (0,3), (1,2), (1,3) S = (0,0), (0,1), (1,0), (1,1), (0,2), (0,3), (1,2), (1,3) S = (R,1,0), (R,1,1) Z = (R,1,0), (R,1,1)



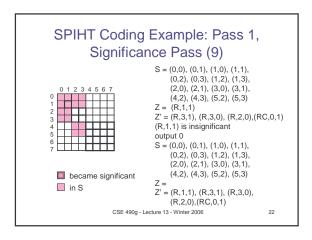




SPIHT Coding Example: Pass 1, Significance Pass (6) S = (0,0), (0,1), (1,0), (1,1), $\begin{array}{ll} (0,2), (0,3), (1,2), (1,3), \\ (2,0), (2,1), (3,0), (3,1) \\ &= (R,2,1), (R,3,0), (R,3,1), (R,1,1) \end{array}$ Z' = (R,2,0),(RC,0,1)(R,2,1) is significant output 1 S = (0,0), (0,1), (1,0), (1,1), (0,2), (0,3), (1,2), (1,3), (2,0), (2,1), (3,0), (3,1), (4,2), (4,3), (5,2), (5,3) output 1010 for signs of these became significant in S Z = (R,3,0), (R,3,1), (R,1,1)Z' = (R,2,0),(RC,0,1)19 CSE 490g - Lecture 13 - Winter 2006



$\begin{array}{c} \text{SPIHT Coding Example: Pass 1,} \\ \text{Significance Pass (8)} \\ \text{S} = (0,0), (0,1), (1,0), (1,1), \\ (0,2), (0,3), (1,2), (1,3), \\ (2,0), (2,1), (3,0), (3,1), \\ (2,0), (2,1), (3,0), (3,1), \\ (4,2), (4,3), (5,2), (5,3) \\ \text{Z} = (R,3,1), (R,1,1) \\ \text{Z'} = (R,3,0), (R,2,0), (RC,0,1) \\ \\ \text{(R,3,1) is insignificant output 0} \\ \text{S} = (0,0), (0,1), (1,0), (1,1), \\ (0,2), (0,3), (1,2), (1,3), \\ (2,0), (2,1), (3,0), (3,1), \\ (4,2), (4,3), (5,2), (5,3) \\ \text{Z} = (R,1,1) \\ \text{I'} = (R,3,1), (R,3,0), (R,2,0), (RC,0,1) \\ \\ \text{CSE 490g - Lecture 13 - Winter 2006} \end{array}$



SPIHT Coding Example: Pass 1, Refinement Step S = (0,0), (0,1), (1,0), (1,1), (0,2), (0,3), (1,2), (1,3), (2,0), (2,1), (3,0), (3,1), (4,2), (4,3), (5,2), (5,3) Z = (R,1,1), (R,3,1), (R,3,0), (R,2,0), (R,2,0), (RC,0,1) output 1011000100000010 one bit for each member of S. 37 total bits in pass 1 were output. Initialization was 4 bits. Total of 41 bits to send 64 bits plus 16 sign bits.

SPIHT Decoding

- The decoder emulates the encoder.
 - The decoder maintains exactly the same data structures as the encoder.
 - When the decoder has popped the Z stack to examine a zero tree it receives a bit telling it whether the tree is significant. The decoder can then do the right thing.
 - If it is significant then it does the decomposition.
 - If it is not significant then it deduces a number of zeros in the current bit plane.

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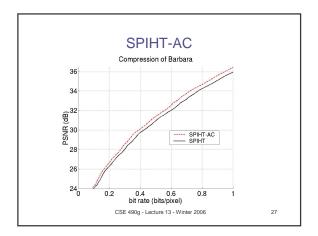
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Notes on SPIHT

- SPIHT was very influential
 - People really came to believe that wavelet compression can really be practical (fast and effective).
- To yield the best compression an arithmetic coding step is added to SPIHT
 - The improvement is about .5 DB

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Group Testing (Dorfman 1943)

- · Given n items, with s items significant
- Use group tests to identify significant items
 - Group test of size k
 - Group is insignificant: all k items insignificant
 - Group is significant: at least one significant
- Goal: Minimize number of group tests

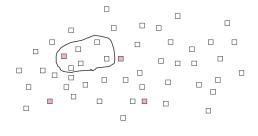
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Group Testing (Dorfman 1943)



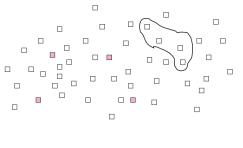
Group Testing (Dorfman 1943)



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Group Testing (Dorfman 1943)



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Group Testing (Dorfman 1943)



Zerotree Coding as Group Testing

- Coefficients = items
- Testing trees for significance = group test
- Zerotree coding = one particular group testing algorithm
- Zerotree coding & group testing have similar goals

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Hwang's Group Testing Algorithm (1972)

- Repeat a Group Iteration until all significant items are found
- Group Interation
 - Test group G containing k unidentified items
 - If G is significant, find a significant item in log_2k tests
 - Each subsequent test is a subset of G
 - Size of test group is halved each time

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Group Iteration of size 8

```
Group Test Result | Code |
| ? ? ? ? ? ? ? ? ? |
| I I I I I I I I
| CSE 490g-Lecture 13 - Winter 2006 | 35
```

Group Iteration of size 8

								Group Test Result	Code
?	?	?	?	?	?	?	?	Significant	1
?	?	?	?	?	?	?	?	Insignificant	0
I	I	Ι	Ι	?	?	?	?	Significant	1
I	I	I	Ι	?	?	?	?	Insignificant	0
I	I	I	I	I	S	?	?		

• Equivalent to elementary Golomb code of order 8

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Group Testing for Wavelet Image Coding (GTW)

- Hong and Ladner (2000)
- New method for encoding significance pass:
 - Uses Hwang's Group Testing Algorithm
 - Divide wavelet coefficients into classes
 - Every group test performed is on coefficients in the same class

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GTW Significance Pass Overview

- · Repeat until all coefficients are coded
 - Pick a set of coefficients from the class that is most likely to have significant coefficients.
 - Do one group iteration on the set. The group size is determined by the adaptive group tester.
 - Output the results of the group tests
 - If a significant coefficient is found then
 - Output its sign
 - Update classes of neighboring coefficients

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GTW's adaptive group tester

- Choosing group iteration size k:
 - Ramp up: start with k=1
 - While group insignificant, double k
 - Steady state: use past history to estimate probability p of insignificance
 - Optimal k using Gallager & Van Voorhis' (1975) result

$$k = \begin{bmatrix} -1/\log_{0} p \end{bmatrix}$$

Same as the adaptive Golomb coding algorithm.

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GTW Classes

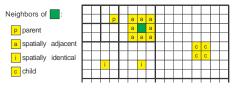
- Coefficients with similar characteristics put into the same class
- Classes are ordered so that classes with coefficients more likely to be significant are tested first.
- Class characteristics
 - Significant neighbor count
 - pattern type
 - Subband level

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Significant Neighbor Metric

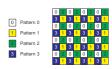
- · Count # of significant neighbors
- · Example Neighborhood



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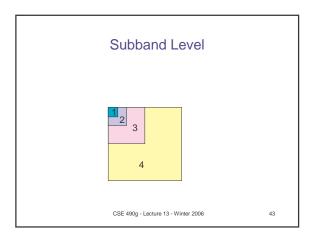
Pattern Type

- Accounts for correlation exists between neighbors
 - Example pattern types for a subband



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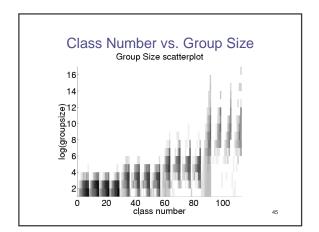
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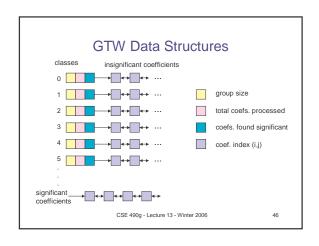


Class Ordering Significant neighbor count - children count for at most 1 - 0,1,2 or 3 or more Pattern Types 4 and Subband levels 7 Total number of classes 112 Ordering - First by significant neighbor count (large to small) - Second by pattern type (small to large) - Third by subband level (small to large)

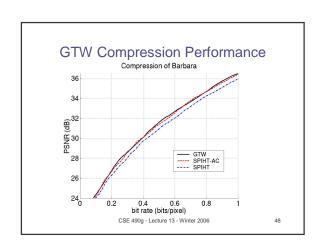
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Decoding • Decoding algorithm is identical to the encoding algorithm except - Decoder knows the results of group test from the compressed bit stream CSE 490g - Lecture 13 - Winter 2006 47



Flexibility of Group Testing

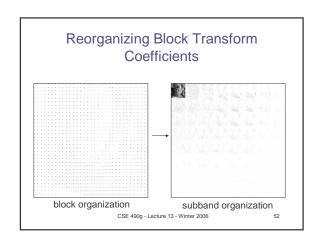
- Flexibility
 - Significant data sent first
 - Classes defined to focus of significant data
 - Data can move from class to class
 - We always get a progressive coder
- Applications
 - DCT
 - Lapped Transforms
 - Wavelet Packets

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GT-DCT

- Hong, Ladner, Riskin (2001)
- Group testing for the discrete cosine transform.
- We do bit-plane coding of the DCT coefficients.
- DCT classes are defined.
- Group testing done first on the classes that have the smallest group size.

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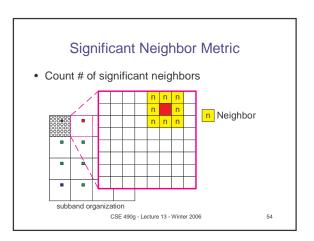


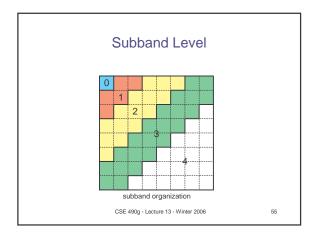
GT-DCT Classes

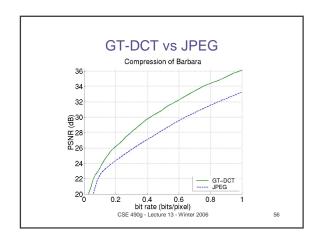
- Based on subband reorganization of coefficients
- · Class characteristics
 - Significant neighbor metric
 - Subband level

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Group Testing Notes

- Group testing provides a unified and flexible way to approach bit-plane coding of transformed images.

 - Need good classes (contexts)
 Need good group testing algorithms (adaptive Golomb coding works)
- Compression performance is outstanding
- Group testing is quite a bit more time consuming than JPEG and SPIHT.
 - need some good data structures and engineering

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