

## Announcements

- Project 2 winners
- Think about Project 3
- Guest lecture on Monday: Aseem

## Multiview stereo

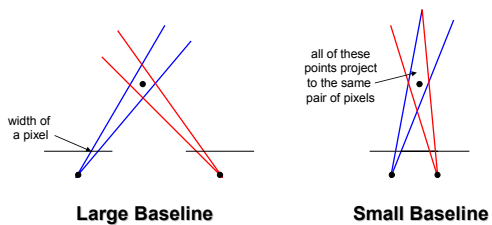


CMU's 3D Room

### Readings

- S. M. Seitz and C. R. Dyer, [Photorealistic Scene Reconstruction by Voxel Coloring](http://www.cs.washington.edu/homes/seitz/papers/ijcv99.pdf), *International Journal of Computer Vision*, 35(2), 1999, pp. 151-173.  
> <http://www.cs.washington.edu/homes/seitz/papers/ijcv99.pdf>

## Choosing the Baseline



### What's the optimal baseline?

- Too small: large depth error
- Too large: difficult search problem

## The Effect of Baseline on Depth Estimation

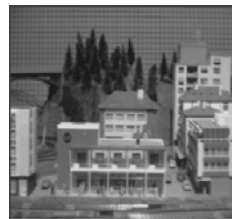
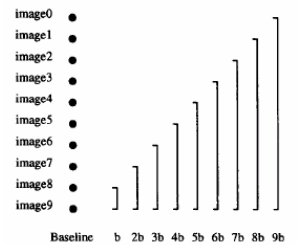


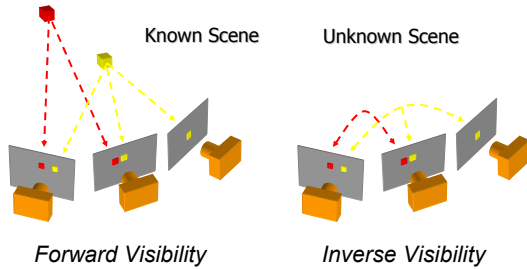
Figure 2: An example scene. The grid pattern in the background has ambiguity of matching.



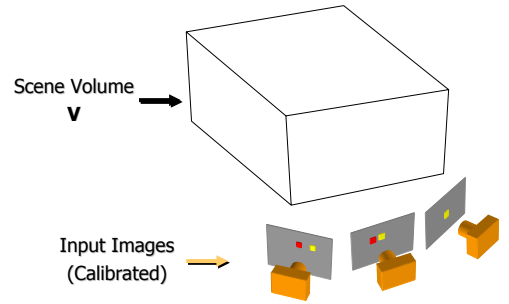


## The visibility problem

Which points are visible in which images?

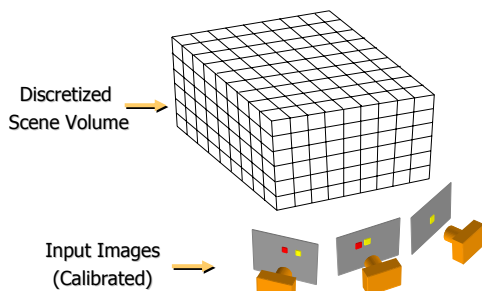


## Volumetric stereo



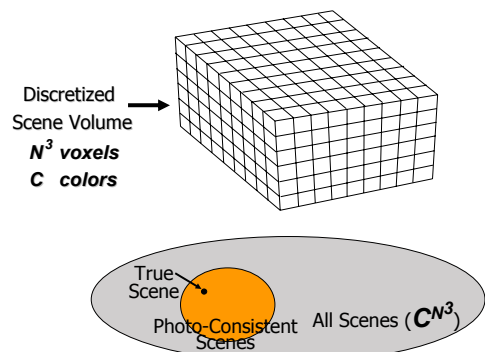
**Goal:** Determine occupancy, "color" of points in  $V$

## Discrete formulation: Voxel Coloring



**Goal:** Assign RGBA values to voxels in  $V$   
*photo-consistent* with images

## Complexity and computability



True Scene  
Photo-Consistent Scenes  
All Scenes ( $C^{N^3}$ )

## Issues

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### Theoretical Questions

- Identify class of *all* photo-consistent scenes

### Practical Questions

- How do we compute photo-consistent models?

## Voxel coloring solutions

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### 1. $C=2$ (shape from silhouettes)

- Volume intersection [Baumgart 1974]
  - > For more info: *Rapid octree construction from image sequences*. R. Szeliski, CVGIP: Image Understanding, 58(1):23-32, July 1993. (this paper is apparently not available online) or
  - > W. Matusik, C. Buehler, R. Raskar, L. McMillan, and S. J. Gortler, *Image-Based Visual Hulls*, SIGGRAPH 2000 ( [pdf 1.6 MB](#) )

### 2. $C$ unconstrained, viewpoint constraints

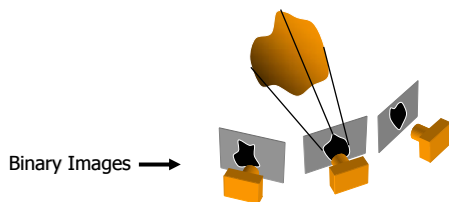
- Voxel coloring algorithm [Seitz & Dyer 97]

### 3. General Case

- Space carving [Kutulakos & Seitz 98]

## Reconstruction from Silhouettes ( $C = 2$ )

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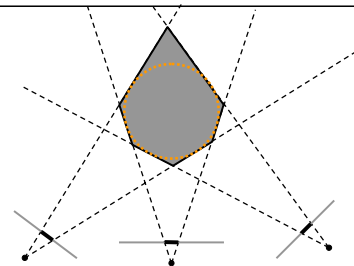


### Approach:

- *Backproject* each silhouette
- Intersect backprojected volumes

## Volume intersection

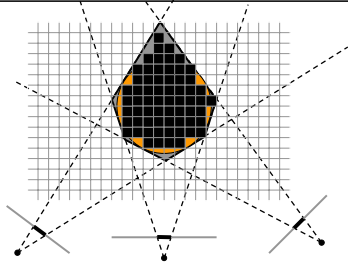
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### Reconstruction Contains the True Scene

- But is generally not the same
- In the limit (all views) get *visual hull*
  - > Complement of all lines that don't intersect  $S$

## Voxel algorithm for volume intersection



Color voxel black if on silhouette in every image

- $O(N^3)$ , for  $M$  images,  $N^3$  voxels
- Don't have to search  $2^{N^3}$  possible scenes!

## Properties of Volume Intersection

### Pros

- Easy to implement, fast
- Accelerated via octrees [Szeliski 1993] or interval techniques [Matusik 2000]

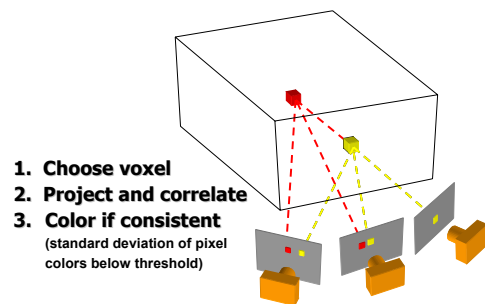
### Cons

- No concavities
- Reconstruction is not photo-consistent
- Requires identification of silhouettes

## Voxel Coloring Solutions

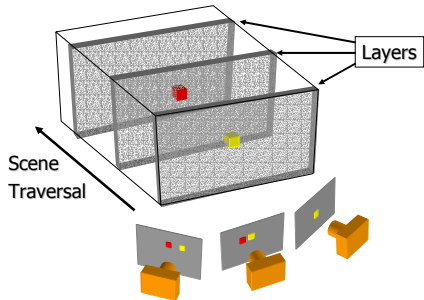
1.  $C=2$  (silhouettes)
  - Volume intersection [Baumgart 1974]
2.  $C$  unconstrained, viewpoint constraints
  - Voxel coloring algorithm [Seitz & Dyer 97]
    - > For more info: <http://www.cs.washington.edu/homes/seitz/papers/icv99.pdf>
3. General Case
  - Space carving [Kutulakos & Seitz 98]

## Voxel Coloring Approach



**Visibility Problem:** in which images is each voxel visible?

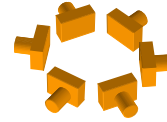
## Depth Ordering: visit occluders first!



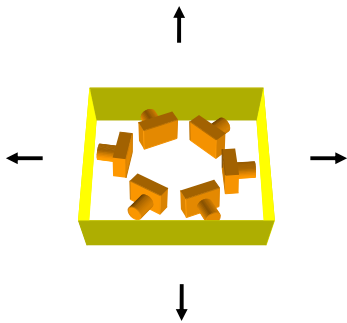
**Condition:** depth order is the *same for all input views*

## Panoramic Depth Ordering

- Cameras oriented in many different directions
- Planar depth ordering does not apply

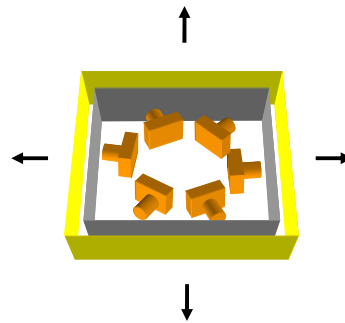


## Panoramic Depth Ordering



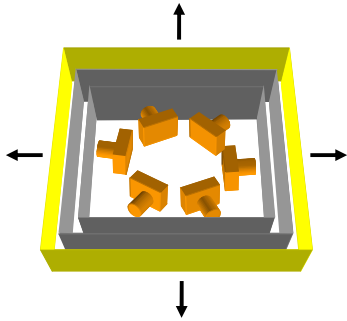
**Layers radiate outwards from cameras**

## Panoramic Layering



**Layers radiate outwards from cameras**

## Panoramic Layering

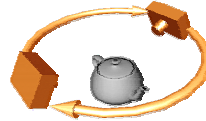


Layers radiate outwards from cameras

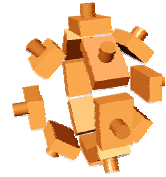
## Compatible Camera Configurations

### Depth-Order Constraint

- Scene outside convex hull of camera centers



*Inward-Looking*

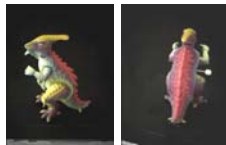


*Outward-Looking*

## Calibrated Image Acquisition



*Calibrated Turntable*



**Selected Dinosaur Images**



**Selected Flower Images**

## Voxel Coloring Results (Video)



### **Dinosaur Reconstruction**

72 K voxels colored  
7.6 M voxels tested  
7 min. to compute  
on a 250MHz SGI

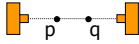


### **Flower Reconstruction**

70 K voxels colored  
7.6 M voxels tested  
7 min. to compute  
on a 250MHz SGI

## Limitations of Depth Ordering

A view-independent depth order may not exist



Need more powerful general-case algorithms

- Unconstrained camera positions
- Unconstrained scene geometry/topology

## Voxel Coloring Solutions

### 1. $C=2$ (silhouettes)

- Volume intersection [Baumgart 1974]

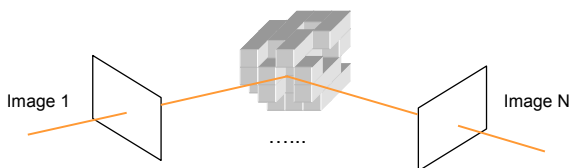
### 2. $C$ unconstrained, viewpoint constraints

- Voxel coloring algorithm [Seitz & Dyer 97]

### 3. General Case

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  - > For more info: <http://www.cs.washington.edu/homes/seitz/papers/kutu-ijcv00.pdf>

## Space Carving Algorithm



### Space Carving Algorithm

- Initialize to a volume  $V$  containing the true scene
- Choose a voxel on the current surface
- Project to visible input images
- Carve if not photo-consistent
- Repeat until convergence

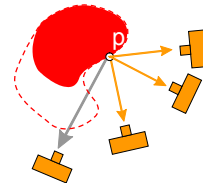
## Convergence

### Consistency Property

- The resulting shape is photo-consistent
  - > all inconsistent points are removed

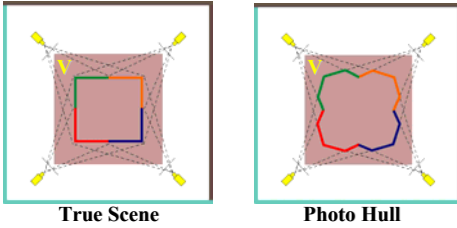
### Convergence Property

- Carving converges to a non-empty shape
  - > a point on the true scene is *never* removed

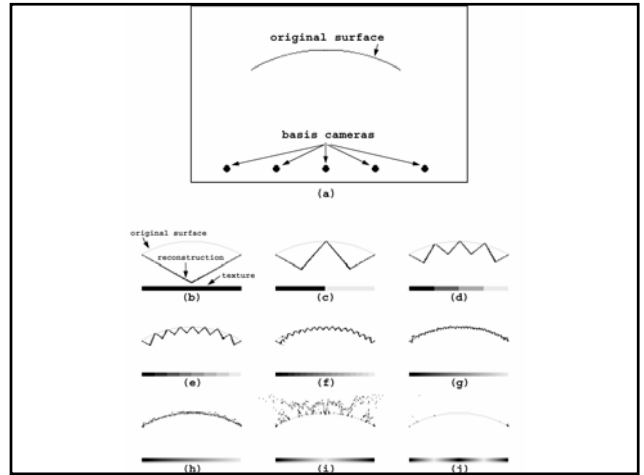




## Which shape do you get?



- The **Photo Hull** is the **UNION** of all photo-consistent scenes in  $V$
- It is a photo-consistent scene reconstruction
  - Tightest possible bound on the true scene



## Space Carving Algorithm

### The Basic Algorithm is Unwieldy

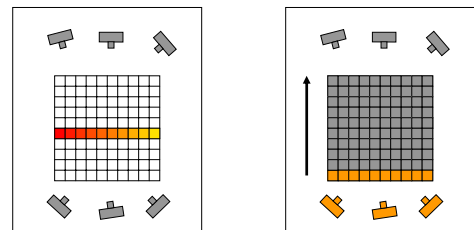
- Complex update procedure

### Alternative: Multi-Pass Plane Sweep

- Efficient, can use texture-mapping hardware
- Converges quickly in practice
- Easy to implement

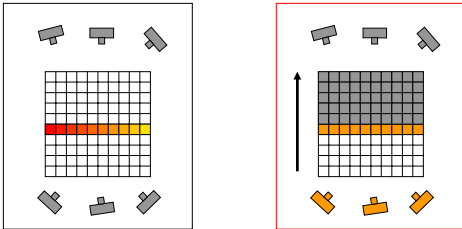
## Multi-Pass Plane Sweep

- Sweep plane in each of 6 principle directions
- Consider cameras on only one side of plane
- Repeat until convergence



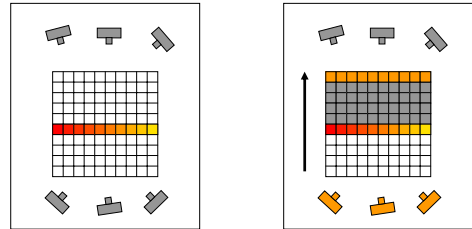
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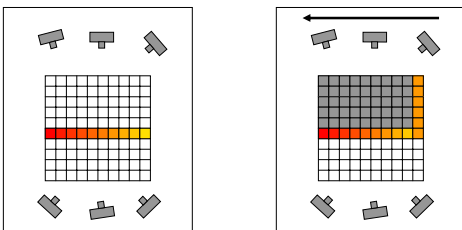
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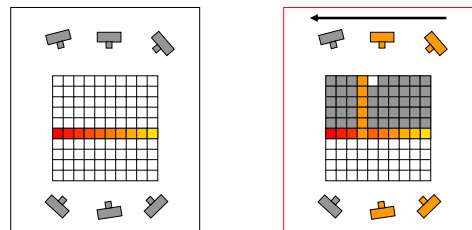
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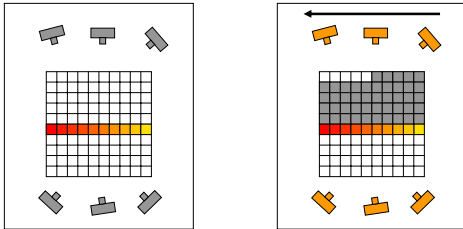
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## Multi-Pass Plane Sweep

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- Consider cameras on only one side of plane
- Repeat until convergence



## Space Carving Results: African Violet



Input Image (1 of 45)



Reconstruction



Reconstruction



Reconstruction

## Space Carving Results: Hand

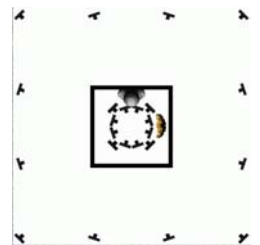


Input Image  
(1 of 100)



Views of Reconstruction

## House Walkthrough



24 rendered input views from inside *and* outside

## Space Carving Results: House



**Input Image**  
(true scene)

**Reconstruction**  
370,000 voxels

## Space Carving Results: House



**Input Image**  
(true scene)

**Reconstruction**  
370,000 voxels

## Space Carving Results: House



**New View (true scene)**

**Reconstruction**



**New View**  
(true scene)

**Reconstruction**

**Reconstruction**  
(with new input view)

## Other Features

### Coarse-to-fine Reconstruction

- Represent scene as octree
- Reconstruct low-res model first, then refine

### Hardware-Acceleration

- Use texture-mapping to compute voxel projections
- Process voxels an entire plane at a time

### Limitations

- Need to acquire calibrated images
- Restriction to simple radiance models
- Bias toward maximal (fat) reconstructions
- Transparency not supported

## Other Approaches

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### Level-Set Methods [Faugeras & Keriven 1998]

- Evolve implicit function by solving PDE's

### Probabilistic Voxel Reconstruction [DeBonet & Viola 1999], [Broadhurst et al. 2001]

- Solve for voxel uncertainty (also transparency)

### Transparency and Matting [Szeliski & Golland 1998]

- Compute voxels with alpha-channel

### Max Flow/Min Cut [Roy & Cox 1998]

- Graph theoretic formulation

### Mesh-Based Stereo [Fua & Leclerc 1995], [Zhang & Seitz 2001]

- Mesh-based but similar consistency formulation

### Virtualized Reality [Narayan, Rander, Kanade 1998]

- Perform stereo 3 images at a time, merge results

## Bibliography

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### Volume Intersection

- Martin & Aggarwal, "Volumetric description of objects from multiple views", Trans. Pattern Analysis and Machine Intelligence, 5(2), 1991, pp. 150-158.
- Szeliski, "Rapid Octree Construction from Image Sequences", Computer Vision, Graphics, and Image Processing: Image Understanding, 58(1), 1993, pp. 23-32.

### Voxel Coloring and Space Carving

- Seitz & Dyer, "Photorealistic Scene Reconstruction by Voxel Coloring", Proc. Computer Vision and Pattern Recognition (CVPR), 1997, pp. 1067-1073.
- Seitz & Kutulakos, "Plenoptic Image Editing", Proc. Int. Conf. on Computer Vision (ICCV), 1998, pp. 17-24.
- Kutulakos & Seitz, "A Theory of Shape by Space Carving", Proc. ICCV, 1998, pp. 307-314.

## Bibliography

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### Related References

- Bolles, Baker, and Marimont, "Epipolar-Plane Image Analysis: An Approach to Determining Structure from Motion", International Journal of Computer Vision, vol 1, no 1, 1987, pp. 7-55.
- DeBonet & Viola, "[Poxels: Probabilistic Voxelized Volume Reconstruction](#)", Proc. Int. Conf. on Computer Vision (ICCV) 1999.
- Broadhurst, Drummond, and Cipolla, "[A Probabilistic Framework for Space Carving](#)", International Conference of Computer Vision (ICCV), 2001, pp. 388-393.
- Faugeras & Keriven, "Variational principles, surface evolution, PDE's, level set methods and the stereo problem", IEEE Trans. on Image Processing, 7(3), 1998, pp. 336-344.
- Szeliski & Golland, "Stereo Matching with Transparency and Matting", Proc. Int. Conf. on Computer Vision (ICCV), 1998, 517-524.
- Roy & Cox, "A Maximum-Flow Formulation of the N-camera Stereo Correspondence Problem", Proc. ICCV, 1998, pp. 492-499.
- Fua & Leclerc, "Object-centered surface reconstruction: Combining multi-image stereo and shading", International Journal of Computer Vision, 16, 1995, pp. 35-56.
- Narayanan, Rander, & Kanade, "Constructing Virtual Worlds Using Dense Stereo", Proc. ICCV, 1998, pp. 3-10.